Scheduling (LNMB Master Course)

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Secretary	Dini Heres-Ticheler Tel.: 053 489 3402
Time	Monday 13.00-14.45 January 24 - March 21 and April 4 - April 18
Location	De Uithof Utrecht, Princetonplein 5, Buys Ballot Laboratorium, Room 106

Information on the web:

http://www.math.utwente.nl/~hurinkjl/sched/

- references
- pdf- and ps-files of the slides of the lectures
- subjects of the course
- news
- ...

Goals

main goals of the course 'Scheduling':

1. get knowledge on basic models in scheduling
2. get knowledge on basic solution techniques for scheduling models
3. learn about applications of scheduling models

Material

- Pinedo, Michael L:
  Planning and Scheduling in Manufacturing and Services;
  Springer Series in Operations Research and Financial Engineering,
  2005, With CD-ROM., Hardcover, ISBN: 0-387-22198-0
- Brucker, Peter: Scheduling Algorithms
  4th ed., 2004, Springer Verlag Berlin, Hardcover, ISBN: 3-540-20524-1
- Pinedo, Michael L: Scheduling: Theory, Algorithms, and Systems;
  2nd ed., 2002, Prentice Hall, ISBN 0-13-028138-7
- handout

Planning of the subjects (temp.)

Lecture	Date	Subject
Lecture 1	24.01.2005	Introduction
Lecture 2	31.01.2005	Single machine models
Lecture 3	07.02.2005	Single machine models
Lecture 4	14.02.2005	Parallel machine models
Lecture 5	21.02.2005	Shop scheduling models
Lecture 6	28.02.2005	Shop scheduling models
Lecture 7	07.03.2005	Shop scheduling models
Lecture 8	14.03.2005	Shop scheduling models
Lecture 9	21.03.2005	Interval scheduling
Lecture 10	04.04.2005	Models in Transportation
Lecture 11	11.04.2005	Models in Transportation
Lecture 12	18.04.2005	open

Structure

- Lectures
  - models
  - methods and algorithms
  - examples
  - applications
- Examination: take home problems
  - will be given on the web-page
  - are updated frequently
  - two series; first to be delivered by 11.03.2005; second by 29.04.2005

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What is Scheduling?

- decision making in manufacturing and service industries
- allocation of scare resources to tasks over time

Two main areas of application

- manufacturing models
- service models

Remark: we only consider deterministic models

Examples: Paper Bag Factory

- factory producing paper bags for different goods
- raw material: rolls of paper
- 3-stage production process
  - printing the logo
  - gluing the sides of the bag
  - sewing one or both ends of the bag
- at each stage several machines for processing
- set of production orders specified by
  - quantity and type of bag
  - committed delivery date

Examples: Paper Bag Factory

- processing times proportional to the quantities
- late delivery leeds to a penalty, magnitude depends on
  - importance of the client
  - tardiness of the delivery
- switching on a machine from production of one bag-type to another, leads to setup time
- objectives:
  - minimize total penalty costs
  - minimize total time spent on setups

Examples: Routing and Scheduling of Airplanes

- airline has a fleet of different aircrafts
- given a set of flights characterized by
  - origin and destination
  - scheduled departure and arrival time
  - customers demand (predicted by the marketing department)
- assigning a particular type of aircraft to a specific flight leg leads to an estimated profit (based on demand)

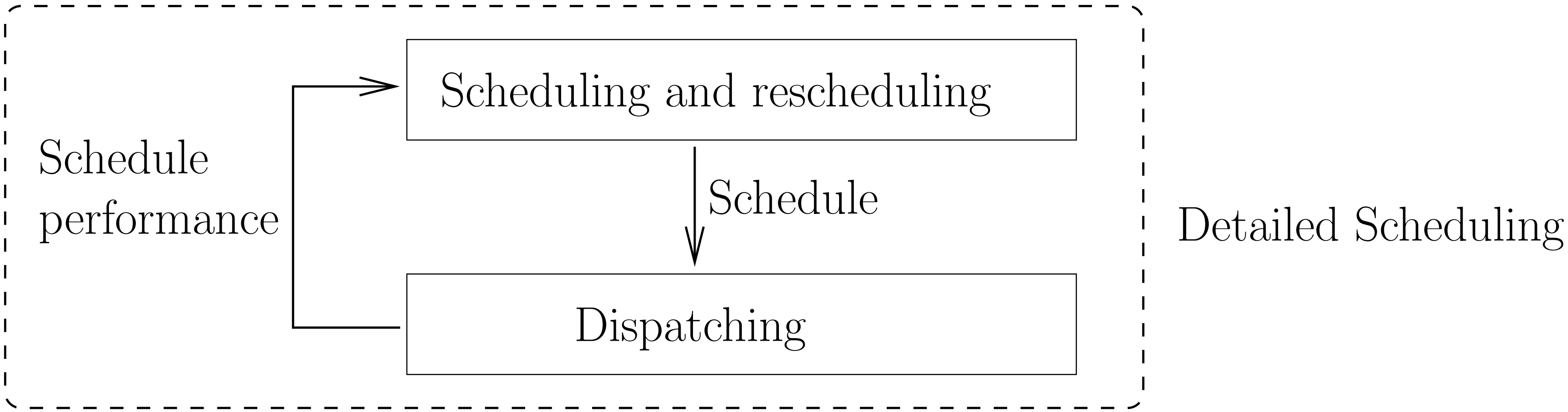
Examples: Routing and Scheduling of Airplanes

- problem: combine different flight legs to round-trips and assign an aircraft to them
- constraints:
  - turn around time at an airport
  - law regulation on duration of a crew duty
  - ...
- goal: maximize profit

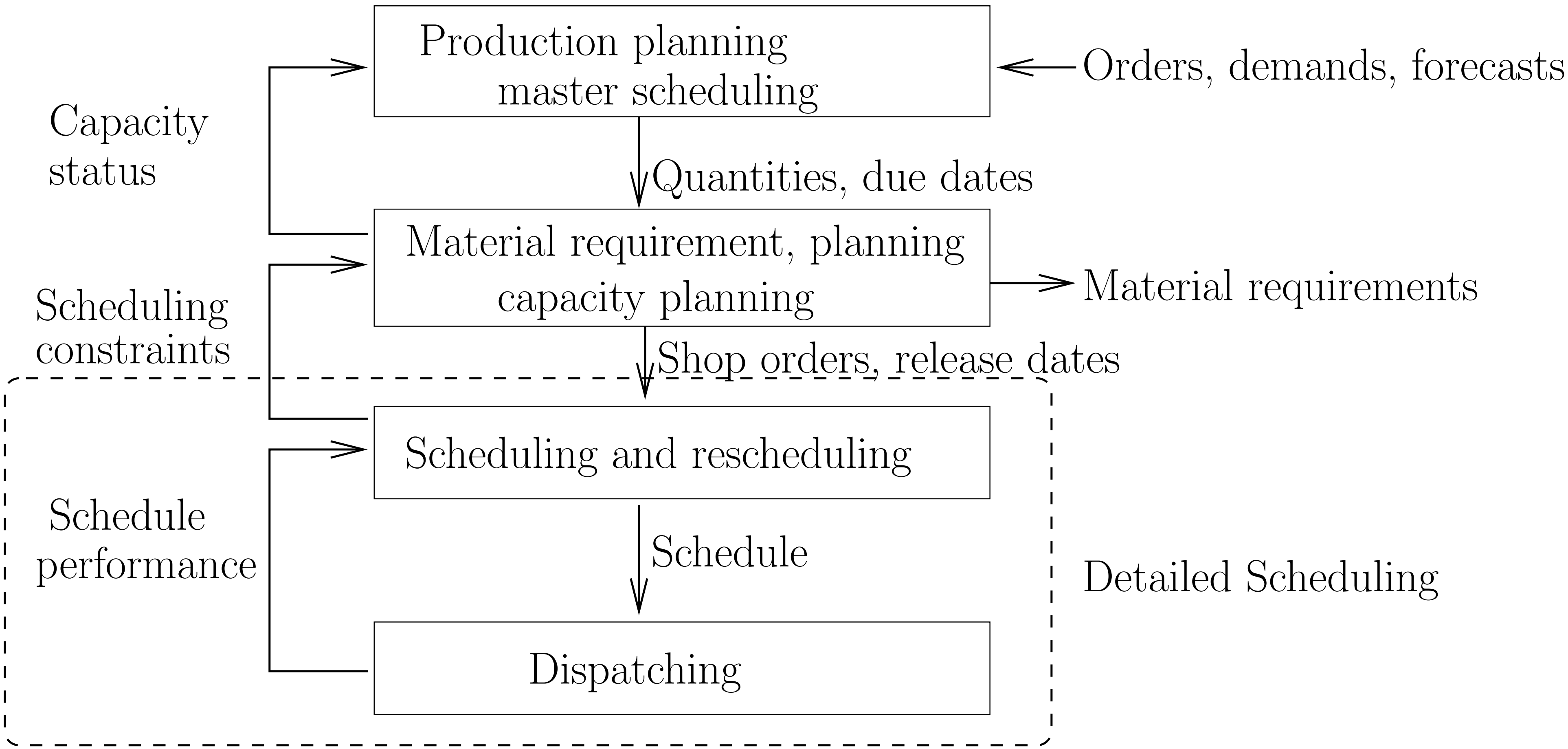
Scheduling Function in an Enterprise

- the scheduling function interacts with many other functions
- interactions are system-dependent
- often take place in an enterprise-wide information system; enterprise resource planning (ERP) system
- often scheduling is done interactively with a decision support system linked to the ERP system

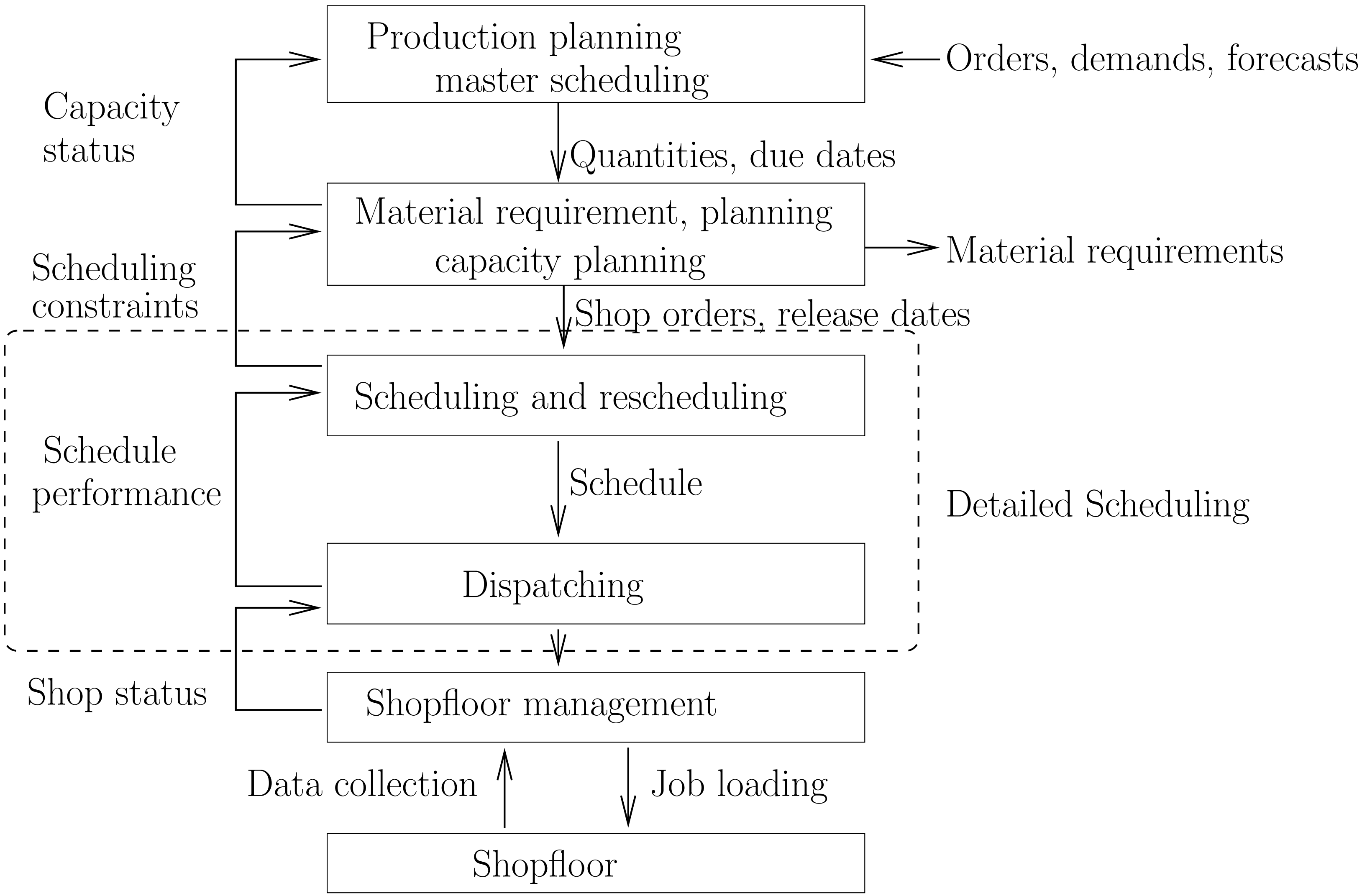
Scheduling in Manufacturing



Scheduling in Manufacturing

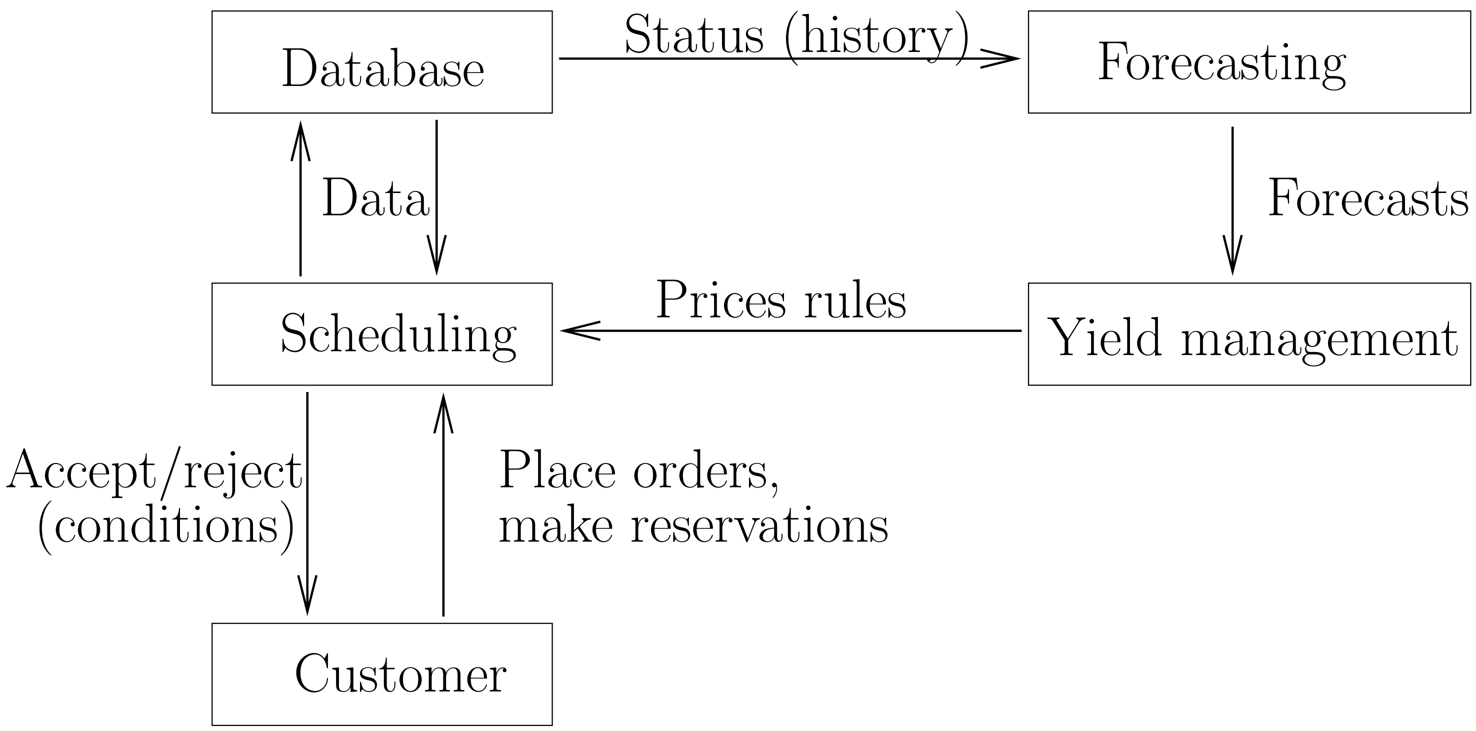


Scheduling in Manufacturing



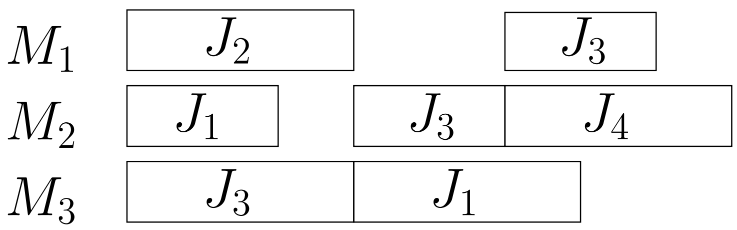
Scheduling in Services

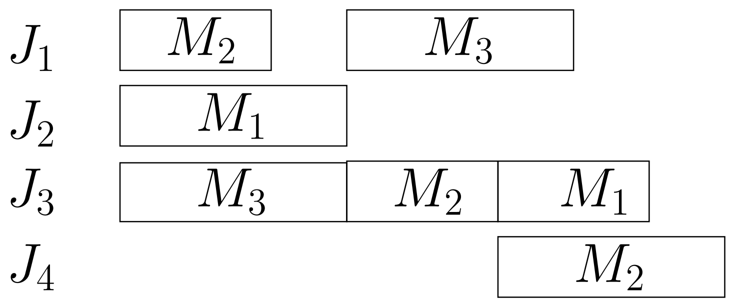
Remark: scheduling function in service organization is much more diverse than in manufacturing



Scheduling models (manufacturing)

- scheduling concerns optimal allocation or assignment of resources, over time, to a set of tasks or activities
  - m machines $M_1, \ldots, M_m$
  - n jobs $J_1, \ldots, J_n$
- schedule may be represented by Gantt charts





Classification of Scheduling Problems

General Notations:

- m machines $1, \ldots, m$
- n jobs $1, \ldots, n$
- (i, j) processing of job j on machine i (called an operation)
- data for jobs:
  - p_{ij}: processing time of operation (i, j)
  - if a job need to be processed only on one machine or has only one operation:
    p_j processing time of job j
  - r_j: release date of job j (earliest starting time)
  - d_j: due date of job j (committed completion time)
  - w_j: weight of job j (importance)

Classification of Scheduling Problems -2-

(Many) Scheduling problems can be described by a three field notation $\alpha|\beta|\gamma$, where

- α describes the machine environment
- β describes the job characteristics, and
- γ describes the objective criterion to be minimized

Remark: A field may contain more than one entry but may also be empty.

Classification - Machine environment

- Single machine ($\alpha = 1$)
- Identical parallel machines ($\alpha = P$ or Pm)
  - m identical machines;
    if $\alpha = P$, the value m is part of the input and if $\alpha = Pm$, the value is considered as a constant (complexity theory)
  - each job consist of a single operation and this may be processed by any of the machines for p_j time units
- Uniform parallel machines ($\alpha = Q$ or Qm)
  - m parallel machines with different speeds $s_1, \ldots, s_m$
  - $p_{ij} = p_j / s_i$
  - each job has to be processed by one of the machines
  - if equal speeds: same situation as for identical machines

Classification - Machine environment -2-

- Unrelated parallel machines ($\alpha = R$ or Rm)
  - m different machines in parallel
  - $p_{ij} = p_j / s_{ij}$, where s_{ij} is speed of job j on machine i
  - each job has to be processed by one of the machines
- Flow Shop ($\alpha = F$ or Fm)
  - m machines in series
  - each job has to be processed on each machine
  - all jobs follow the same route: first machine 1, then machine 2, etc
  - if the jobs have to be processed in the same order on all machines, we have a **permutation** flow shop

Classification - Machine environment

- Flexible Flow Shop ($\alpha = FF$ or FFm)
  - a flow shop with m stages in series
  - at each stage a number of machines in parallel
- Job Shop ($\alpha = J$ or Jm)
  - each job has its individual predetermined route to follow
  - a job does not have to be processed on each machine
  - if a job can visit machines more than once, this is called **recirculation** or **reentrance**
- Flexible Job Shop ($\alpha = FJ$ or FJm)
  - machines replaced by work centers with parallel identical machines

Classification - Machine environment

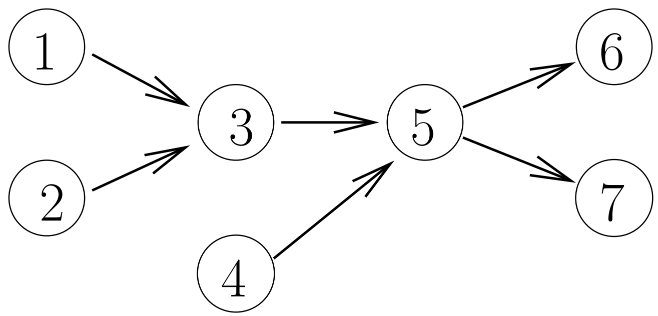
- Open Shop ($\alpha = O$ or Om)
  - each job has to be processed on each machine once
  - processing times may be 0
  - no routing restrictions (this is a scheduling decision)

Classification - Job characteristics

- release dates (r_j is contained in β field)
  - if r_j is not in β field, jobs may start at any time
  - if r_j is in β field, jobs may not start processing before their release date r_j
- preemption (*pmtn* or *prmp* is contained in β field)
  - processing of a job on a machine may be interrupted and resumed at a later time even on a different machine
  - the already processed amount is not lost
- unit processing times ($p_j = 1$ or $p_{ij} = 1$ in β field)
  - each job (operation) has unit processing times
- other 'obvious' specifications (i.e. $d_j = d$)

Classification - Job characteristics -2-

- precedence constraints (*prec* in β field)
  - between jobs precedence relations are given: a job may not start its processing before another job has been finished
  - may be represented by an acyclic graph (vertices = jobs, arcs = precedence relations)



  - special forms of the precedences are possible: if the graph is a chain, intree or outtree, *prec* is replaced by *chain*, *intree* or *outtree*

Classification - Objective criterion

Notations:

- C_{ij}: completion time of operation (i, j)
- C_j: completion time of job j (= completion time of last operation)
- $L_j = C_j - d_j$: lateness of job j
- $T_j = \max\{C_j - d_j, 0\}$: tardiness of job j
- $U_j = \begin{cases} 1 & \text{if } C_j > d_j \\ 0 & \text{otherwise} \end{cases}$: unit penalty

Classification - Objective criterion

- Makespan ($\gamma = C_{max}$)
  - $C_{max} = \max\{C_1, \ldots, C_n\}$
- Maximum lateness ($\gamma = L_{max}$)
  - $L_{max} = \max\{L_1, \ldots, L_n\}$
- Total completion time ($\gamma = \sum C_j$)
  - can be used to measure the Work-In-Progress (WIP)
- Total weighted completion time ($\gamma = \sum w_j C_j$)
  - represents the weighted flow times of the jobs
- Total (weighted) tardiness ($\gamma = \sum (w_j) T_j$)
- (weighted) number of tardy jobs ($\gamma = \sum (w_j) U_j$)

Remark: the mentioned classification gives only an overview of the basic models; lots of further extensions can be found in the literature!